

**Reinstating Floyd-Steinberg:  
Improved Metrics for Quality Assessment  
of Error Diffusion Algorithms**

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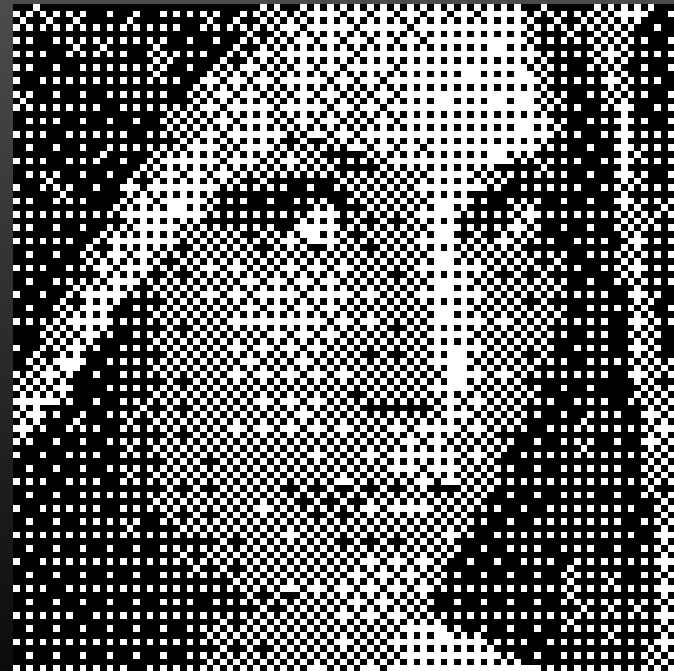
# Introduction

- Halftoning is the process of converting a continuous tone image into another image with a reduced number of tones.



# Ordered dithering

- Tiles a dither matrix (eg. Bayer, void-and-cluster) for use as threshold values.
- Average quality, fast, parallelisable.



# Error diffusion

- Uses feedback through an error diffusion matrix (eg. Floyd-Steinberg, Stucki, JaJuNi...).
- Good quality, hardly parallelisable.



# Direct binary search

- Uses a human visual system model to simulate eye behaviour and minimise a global distance.
- Excellent quality, yet very slow (iterative).



# What is “quality”?

- One possible metric:

$$E(h, b) = \frac{(\|v * h_{i,j} - v * b_{i,j}\|_2)^2}{wh}$$

- $h$ : original image
  - $b$ : dithered image
  - $v$ : human visual system filter
- Smaller error = higher quality

# The human visual system model



# Relative quality of algorithms

- Using *lena.tga* and a Gaussian HVS:

- 8×8 Bayer dithering:

$$E = 0.06352$$

- Floyd-Steinberg dithering:

$$E = 0.01847$$

- Direct binary search:

$$E = 0.00984$$

- Other images show a similar trend

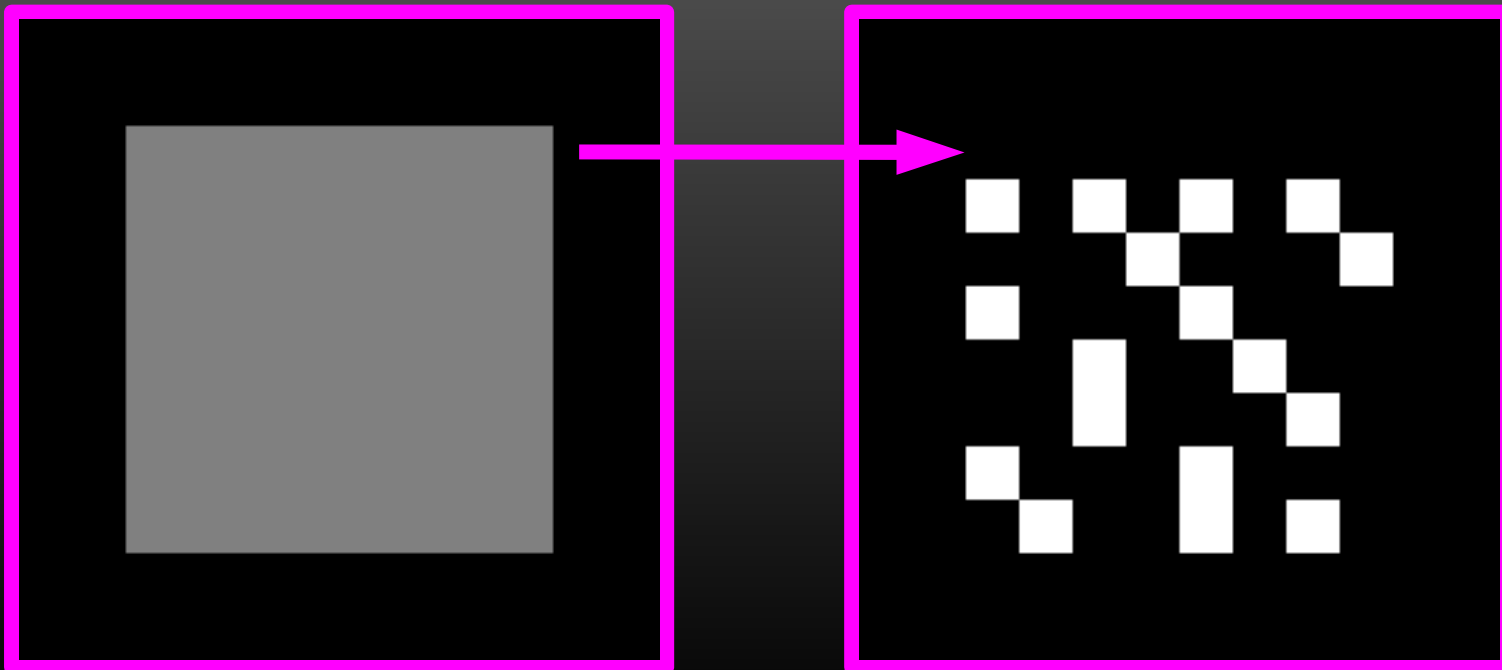


# Image displacement

- Floyd-Steinberg kernel:
- Error is propagated to the

$$\frac{1}{16} \begin{vmatrix} - & x & 7 \\ 3 & 5 & 1 \end{vmatrix}$$

right and bottom, which shows in the image:



# Image displacement

- Slight formula modification:

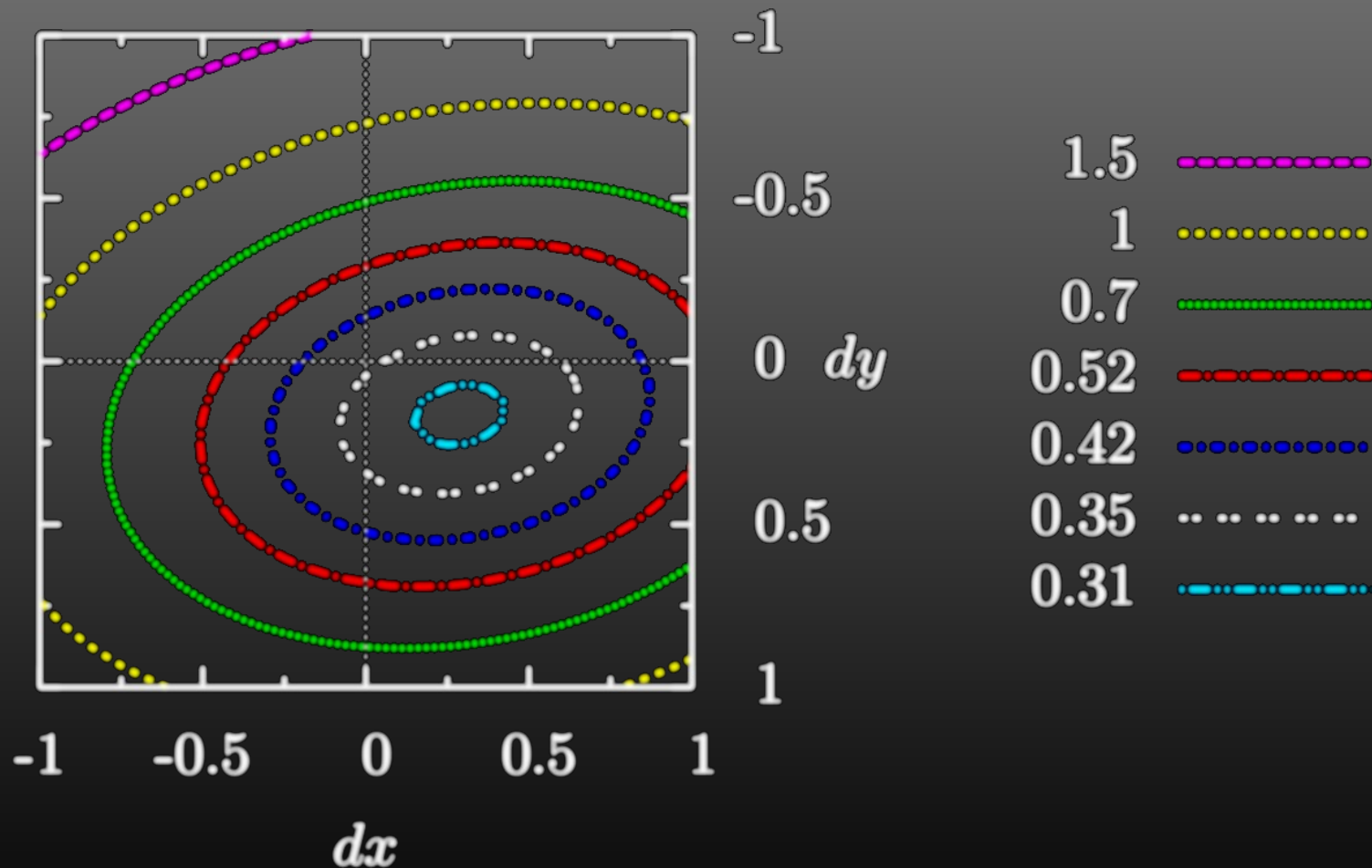
$$E_{dx,dy}(h, b) = \frac{(\|v * h_{i,j} - v * t_{dx,dy} * b_{i,j}\|_2)^2}{wh}$$

–  $t_{dx,dy}$  translates the image by  $(dx, dy)$

- For most error-diffused images,  $E_{dx,dy}$  has a local minimum  $E_{min}$  which is not  $(0, 0)$
- $E_{min}$  is our new quality metric

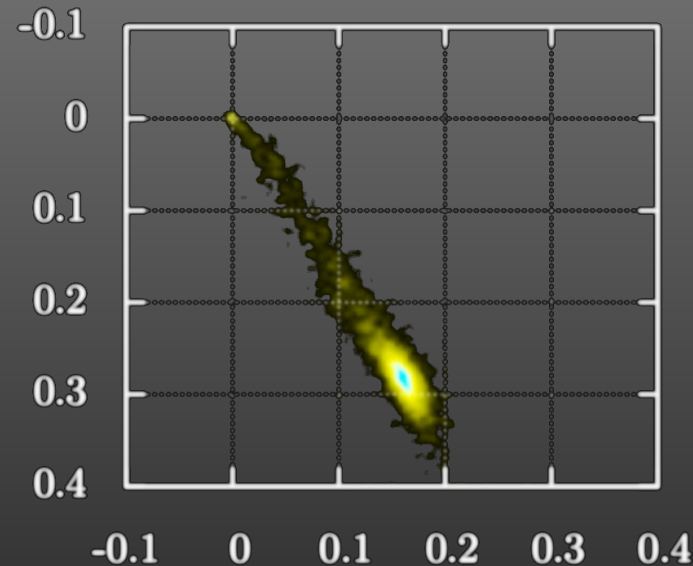
# $E_{dx,dy}$ variations for *lena.tga*

- F-S displacement for *lena.tga* is (0.28, 0.22):



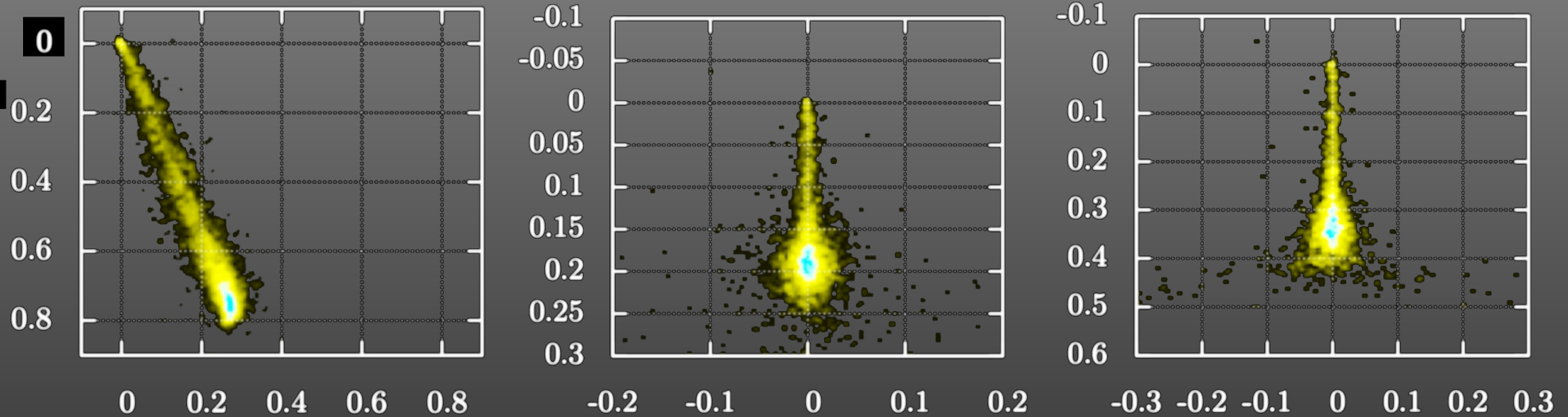
# $(dx, dy)_{min}$ variations

- Histogram on a sample of 10,000 images:



- Floyd-Steinberg *displacement* is  $(0.16, 0.28)$
- We introduce  $E_{fast} = E_{0.16, 0.28}$  which is statistically a better metric than  $E$ .

# Displacement for other algorithms



- Jarvis-Judice-Ninke: (0.26, 0.76)
- Ostromoukhov: (0.0, 0.19)
- Serpentine optimum: (0.0, 0.34)

# Application: improving Floyd-Steinberg

- The idea: find the best Floyd-Steinberg-like diffusion kernel by computing  $E_{min}$  for many sample images and diffusion kernels
- We use *CPUShare* ([www.cpushare.com](http://www.cpushare.com)) for cheap and secure distributed computing

# Results

- Result #1: best kernel is {6, 3, 5, 2}, original Floyd-Steinberg {7, 3, 5, 1} is 2<sup>nd</sup> best
- Result #2: using  $E$  instead of  $E_{min}$  elects poor kernels such as {7, 3, 6, 0}
- Result #3: {7, 4, 5, 0} is a much better kernel for serpentine scan than the original Floyd-Steinberg

# Future work

- Find a link between  $(dx, dy)_{min}$  and the ED kernel
- Optimise other widely-used ED kernels
- Experiment with more complex HVS models



